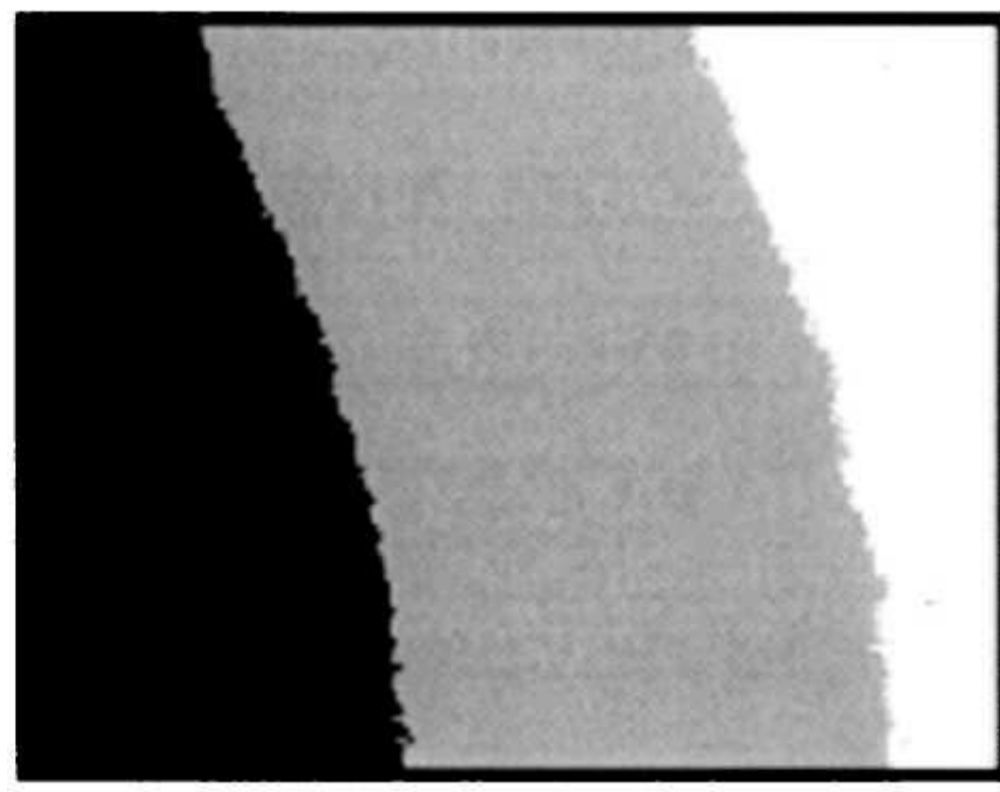


## Abstract

We examine the dynamics of a domain wall subject to a pinning potential, in situations where the position of the wall is coupled to an internal degree of freedom (e.g. a spin phase, in magnetic domain walls). We investigate the corresponding depinning transition, which displays several novel features when compared to standard cases. At zero temperature, there exists a bistable regime for low forces, with a logarithmic behavior close to the transition. For weak pinning, there occurs a succession of bistable transitions corresponding to different modes of the phase evolution, separated by topological transitions. At finite temperature, using techniques from stochastic dynamical systems, we show that the force-velocity characteristics is non-monotonous, as an effect of the zero-temperature topological transitions [1]. We compare our results to recent experiments [2] on permalloy nanowires.

## Interfaces & depinning transition



from Lemerle et al., PRL 80 849 (1998)

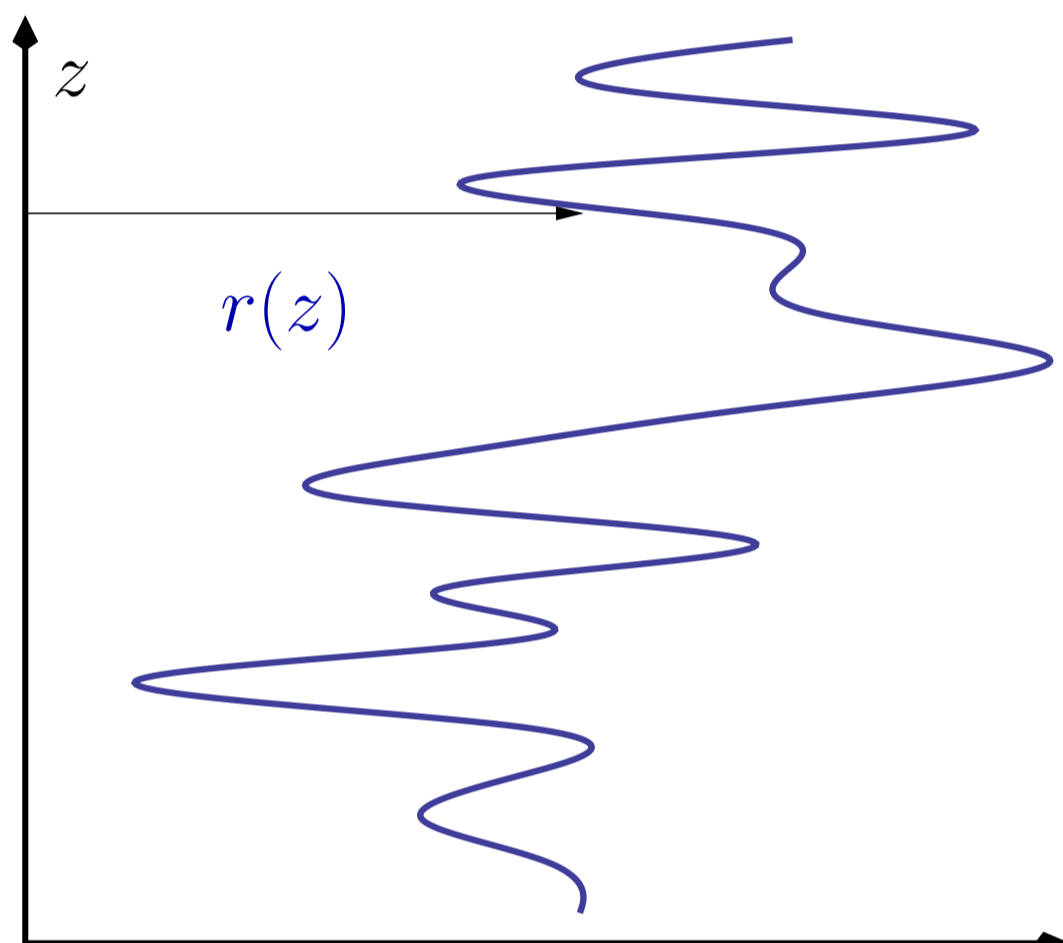
### Examples of interfaces:

- ★ magnetic domain wall (figure on the left)
- ★ contact line
- ★ growth interface
- ★ propagating crack

→ large variety of time and space scales

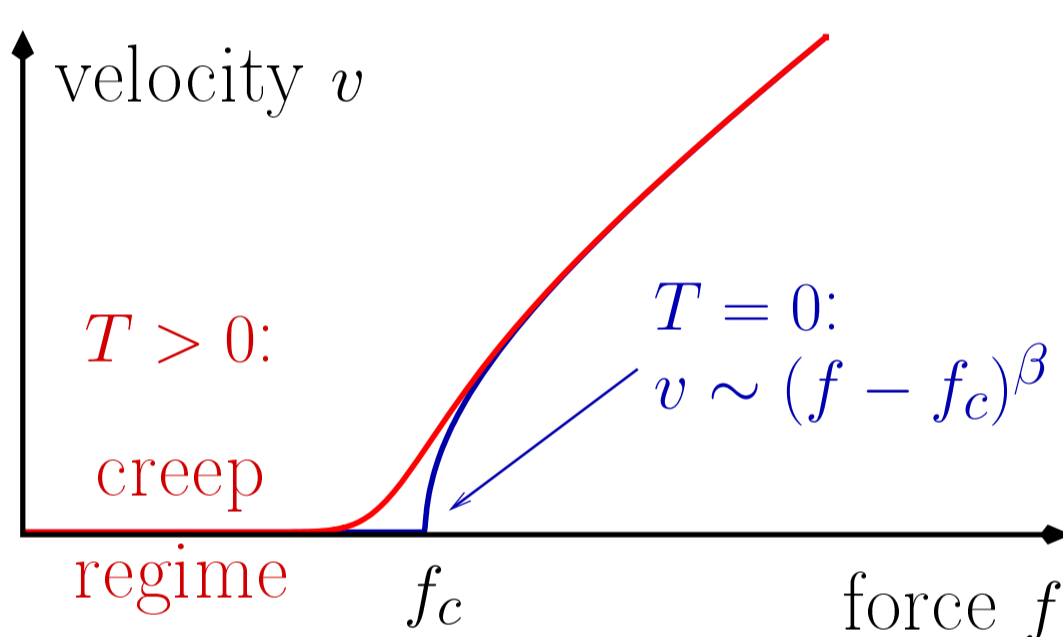
### Common underlying description of interfaces:

- ★ complex object described by its mere position  $r(z)$
  - ★ elasticity tends to **flatten** the interface
  - ★ disorder tends to **deform** it
- competition btw “order” and “disorder”  
nontrivial landscape of energy  
yielding metastability, roughness, pinning



### Depinning transition:

- ★ at  $T = 0$ : pinning up to a critical force  $f_c$
- ★ depinning above  $f_c$ , reminiscent of static phase tr.
- ★ BUT: depinning is **dynamical**
- ★ at  $T > 0$ : creep, thermal rounding



## Question & model

### • Is $r(z)$ containing enough information?

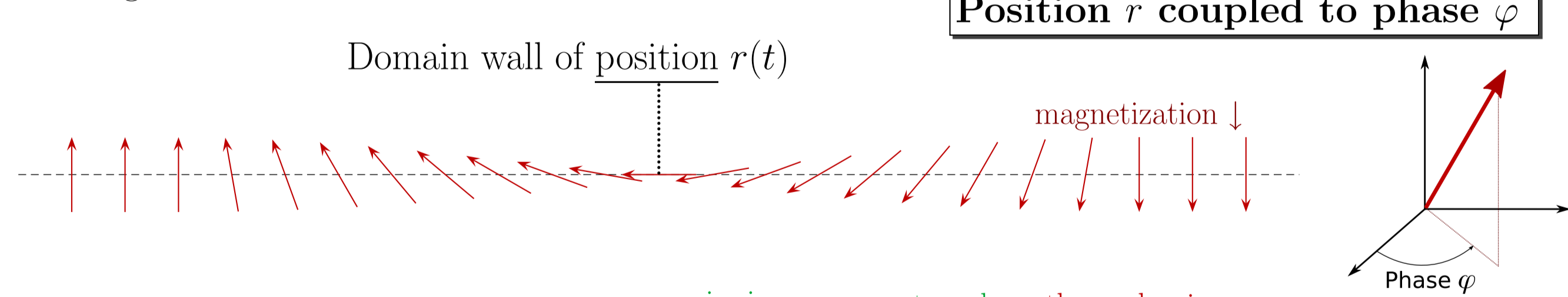
→ examine models with  $r$  coupled to an internal degree of freedom  $\varphi$

$$(\partial_t r, \partial_t \varphi) = f_{\text{pinning}}(r, \varphi) + f_{\text{ext}}$$

### • Example situations:

- ★ underdamped motion in a periodic potential [3]
- ★ viscously coupled elastic manifolds [4]
- ★ domain walls in ferromagnetic materials [5]

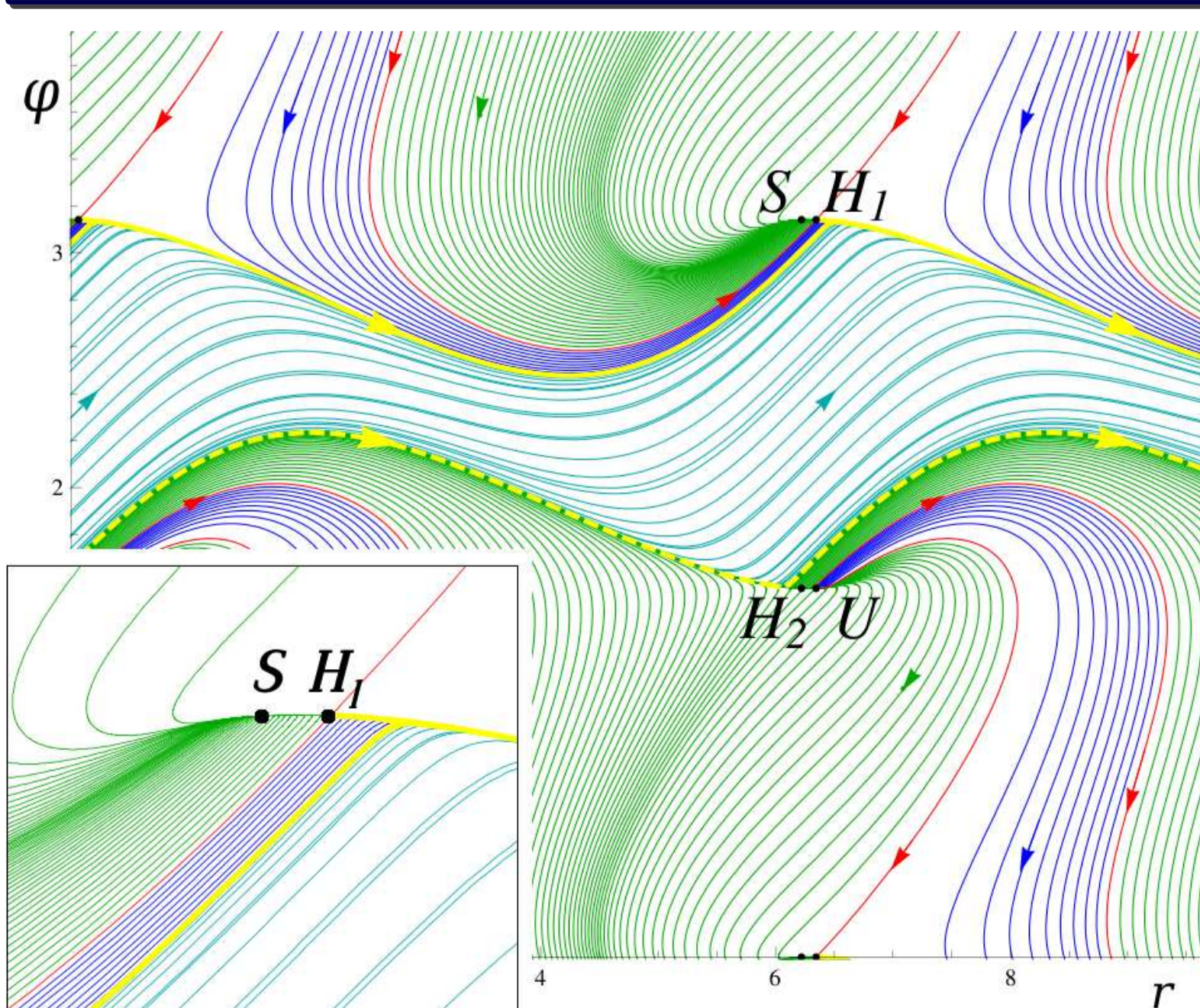
### • Ferromagnetic wire:



effective equations [6]:

$$\begin{cases} \alpha \partial_t r - \partial_t \varphi = -\frac{\text{pinning}}{\cos \kappa r} + \frac{\text{external}}{f} + \frac{\text{thermal noise}}{\eta_1} \\ \alpha \partial_t \varphi + \partial_t r = -\frac{1}{2} K_{\perp} \sin 2\varphi + \eta_2 \end{cases}$$

## Phase space



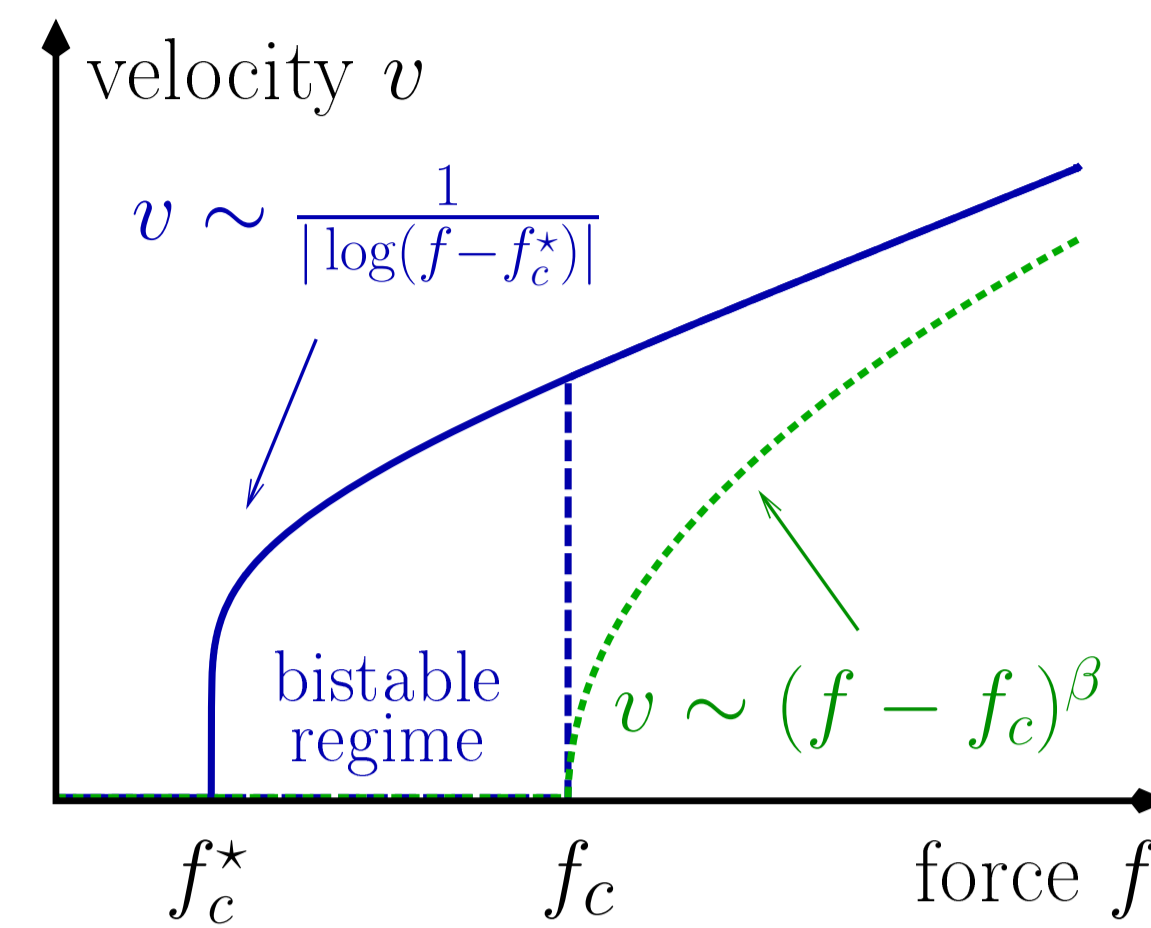
For some regime of force, **bistability** occurs.

Trajectories in the periodic  $(r, \varphi)$  phase space

- are determined through the fixed points:
  - ★  $S$  is stable (attractive)
  - ★  $U$  is unstable (repulsive)
  - ★  $H_1$  and  $H_2$  are hyperbolic (stable+unstable directions)
- and split into those
  - ★ ending at  $S$  (having  $v = 0$ ) (green)
  - ★ rolling to the **limit circle** (turquoise, blue) (having  $v > 0$ )

At  $f = f_c^*$  occurs a homoclinic bifurcation.

## Results at zero temperature



### Dramatic change in the depinning law:

- ★  $v \sim \frac{1}{|\log(f-f_c^*)|} \neq$  the standard  $v \sim (f-f_c^*)^\beta$
- ★ bistable regime for  $f_c^* < f < f_c$

### Interpretation: for $f_c^* < f < f_c$ , the wall is

- ★ either pinned
- ★ or  $r$  slides down its tilted potential while  $\varphi$  oscillates around its own minimum, helping  $r$  to cross its barriers

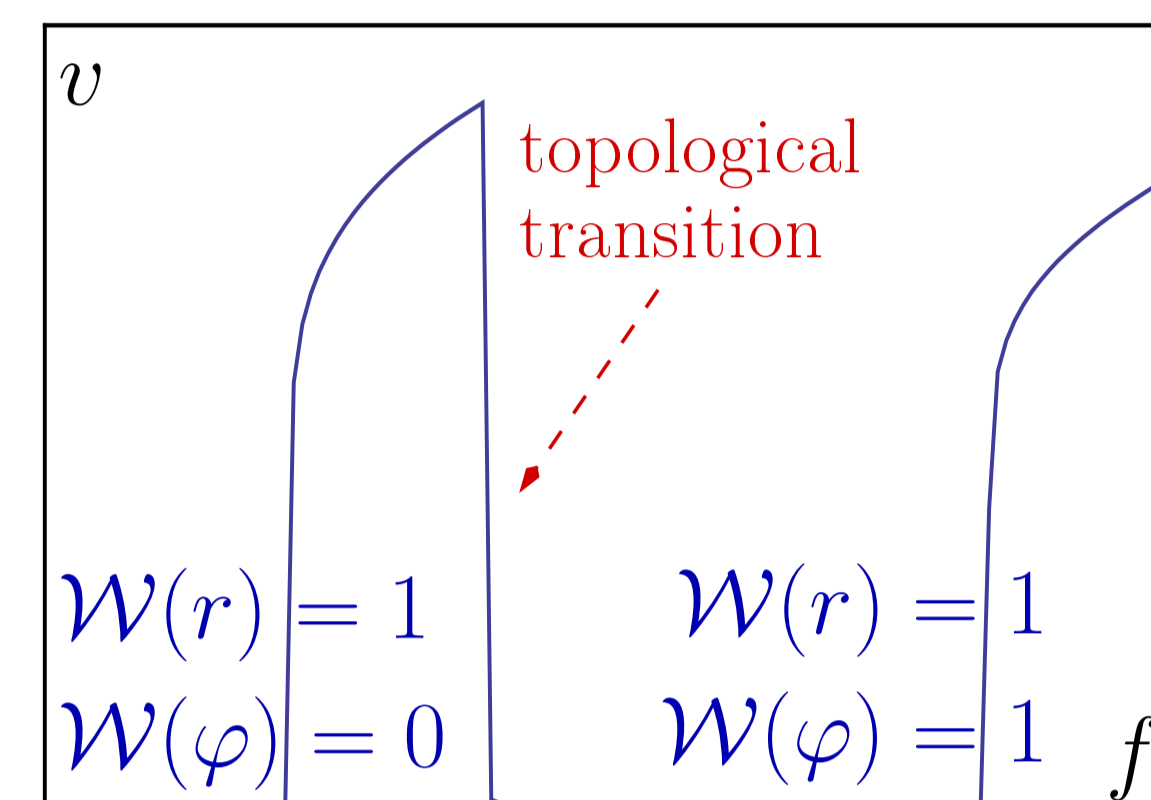
→  $\varphi$  plays the rôle of **inertia**

### Topological transition:

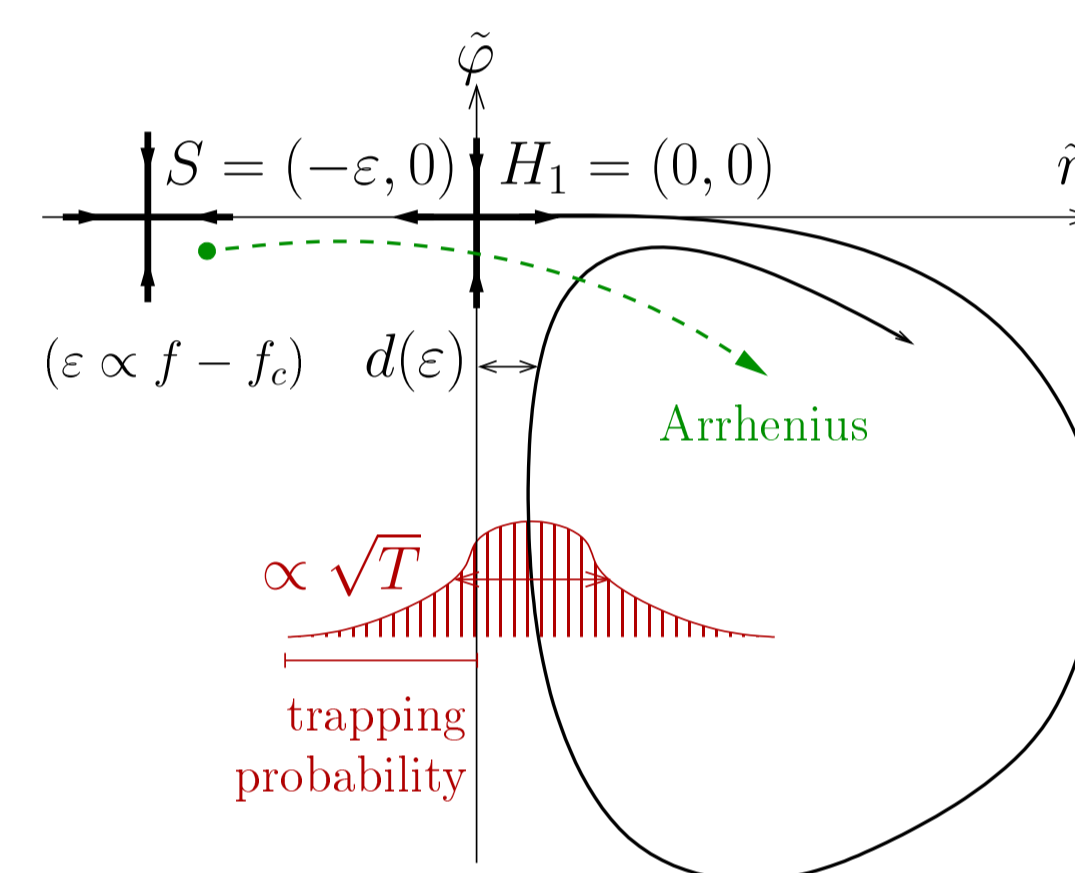
- ★ successive regimes
- ★ characterized by winding numbers  $\mathcal{W}$

### Interpretation: increasing $f$ ,

- ★  $\varphi$  crosses its barrier and falls into its minimum
- ⇒ dissipation increases and  $\varphi$  cannot help  $r$  anymore
- ★ at larger  $f$ : revival with both  $r$  and  $\varphi$  increasing

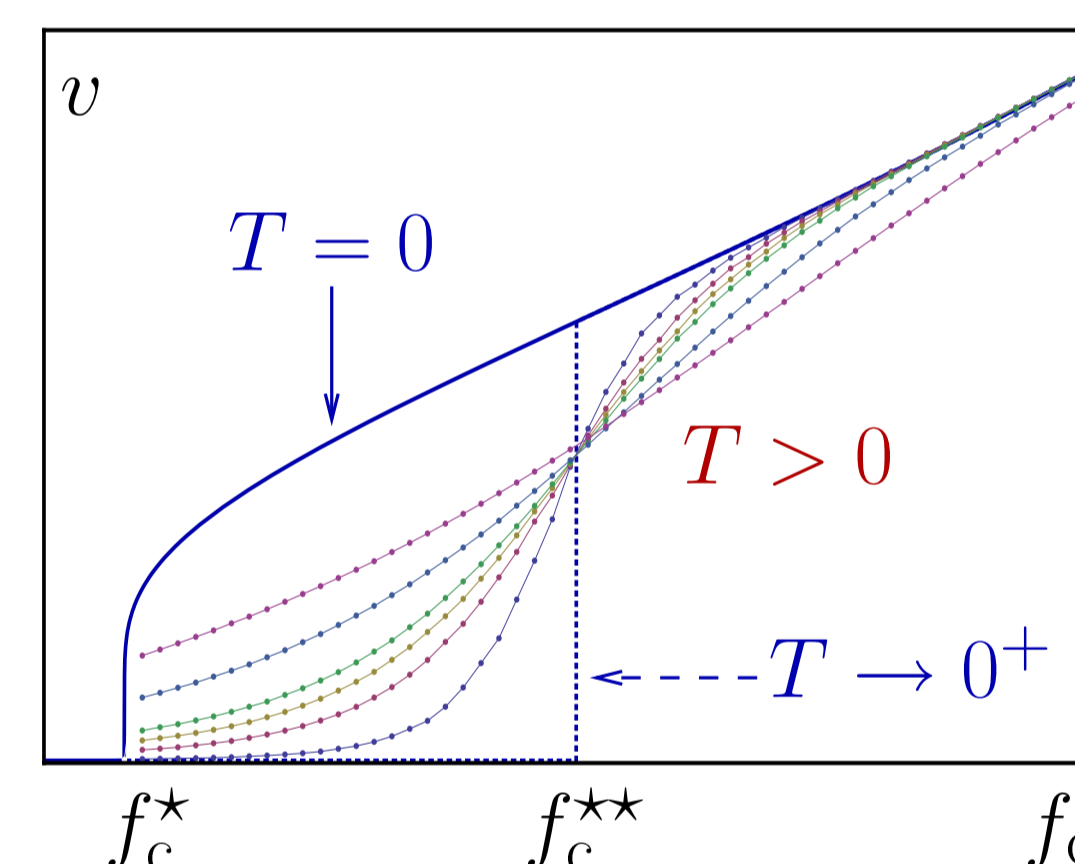


## Results at finite temperature



$$\text{velocity} \sim \frac{\text{characteristic length}}{\text{escape time}}$$

$$\text{escape time} \sim \underbrace{\exp\left(\frac{\varepsilon_c^3}{T}\right)}_{\text{Arrhenius}} \underbrace{\exp\left(-\frac{A}{T}(\varepsilon - \varepsilon_c)^2\right)}_{\text{trapping probability}}$$



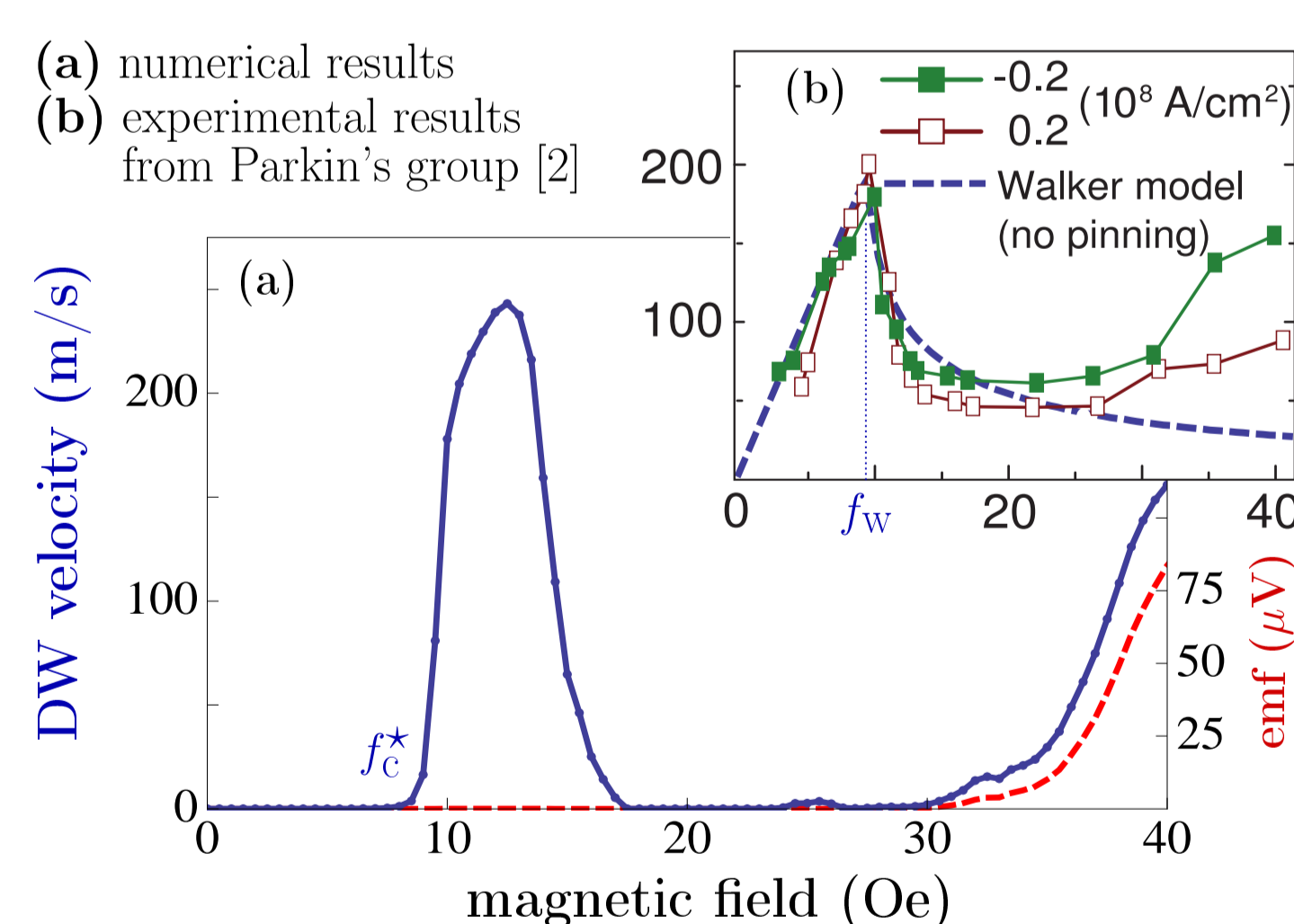
### Depinning law $v(f)$ at finite temperature:

- ★ all curves cross at fixed force  $f_c^{**}$
- ★ contrasts with standard thermal rounding
- ★ in the  $T \rightarrow 0^+$  limit:  $v(f)$  is discontinuous in  $f_c^{**}$

### Topological transition at finite temperature:

the depinning law  $v(f)$  is **non-monotonous**

## Comparison to experiment



- Experimental results [2]: non-monotonous  $v(f)$  with two peaks
- Walker's model [5] (no pinning potential): only one peak
- Our results (simple pinning potential):
  - ★ two peaks in  $v(f)$  for reasonable parameters
  - ★ prediction: the **emf** ( $\propto \langle \dot{\varphi} \rangle$ ) increases at the second peak

## Conclusion & outlook

### Effect of coupling to an internal degree of freedom:

- ★ unusual depinning law
- ★ bistability
- ★ non-monotonous  $v(f)$  at finite  $T$
- ★ link with experiments

### Perspective:

- ★ Current driven wall
- ★ Interface with elasticity
- modified creep law?
- ★ Experiments: periodic patterning

## References

- [1] Lecomte V, Barnes SE, Eckmann J-P, Giamarchi T, *PRB* 80 054413 (2009)
- [2] Parkin SSP *et al.*, *Science* 320 190 (2008)
- [3] Vollmer HD, Risken H, *Z. Phys. B* 37 343 (1980)
- [4] Le Doussal P, Marchetti MC, *PRB* 78 224201 (2008)
- [5] Schryer NL, Walker LR, *J. Applied Phys.* 45 5406 (1974)
- [6] Duine RA, Morais-Smith C, *PRB* 77 094434 (2008)